

BOTH L & R

HIP

KNEE



0

0



180

0



0

180



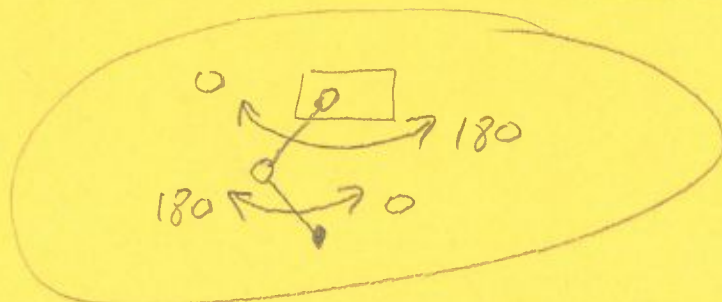
180

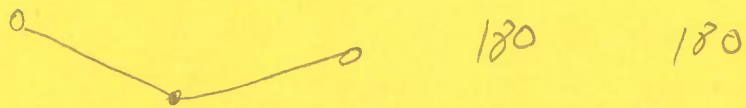
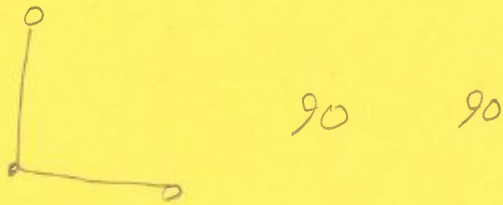
180



90

90





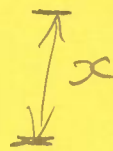
5/10



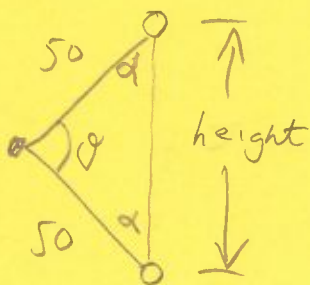
45/90



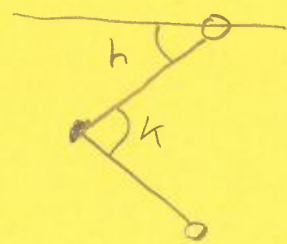
90/180



!

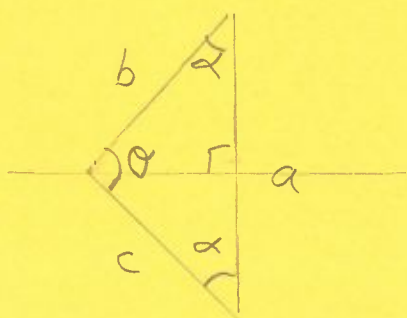
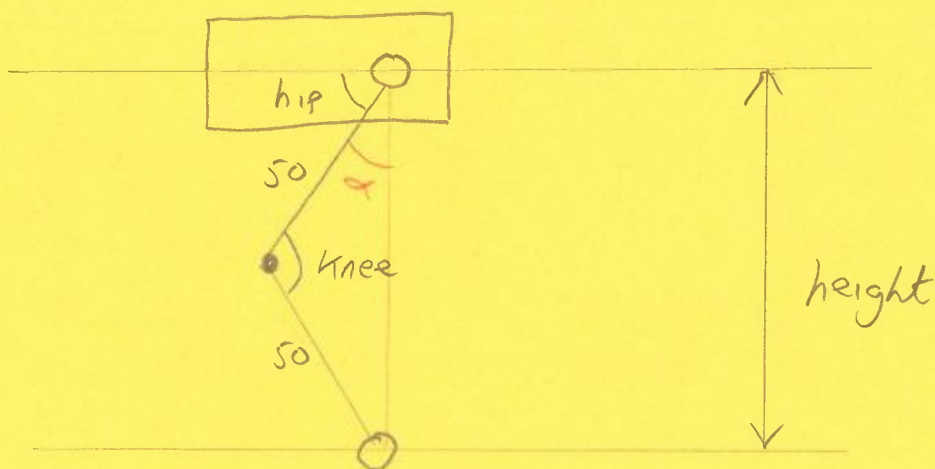


hip angle h



knee angle k

I



$$\theta = \cos^{-1} \left[\frac{(b^2 + c^2 - a^2)}{2bc} \right]$$

$$\alpha = \frac{180 - \theta}{2} = 90 - \frac{\theta}{2}$$

II

$$\text{knee} = \cos^{-1} \left[\frac{(50^2 + 50^2 - \text{height}^2)}{2 \times 50 \times 50} \right]$$

$$= \cos^{-1} \left[\frac{(5000 - \text{height}^2)}{5000} \right]$$

$$= \cos^{-1} \left[\frac{5000 - \text{height}^2}{5000} \right]$$

$$= \cos^{-1} \left[1 - \frac{\text{height}^2}{5000} \right]$$

$$\alpha = 90 - \frac{\text{knee}}{2}$$

$$\text{hip} = 90 - \alpha$$

$$= 90 - \left(90 - \frac{\text{knee}}{2} \right)$$

$$= + \frac{\text{knee}}{2}$$

(B)

$$\alpha' = \frac{180 - \theta'}{2}$$

$$= 90 - \frac{\theta'}{2}$$

$$\text{hip}' = 90 - \alpha' - \beta'$$

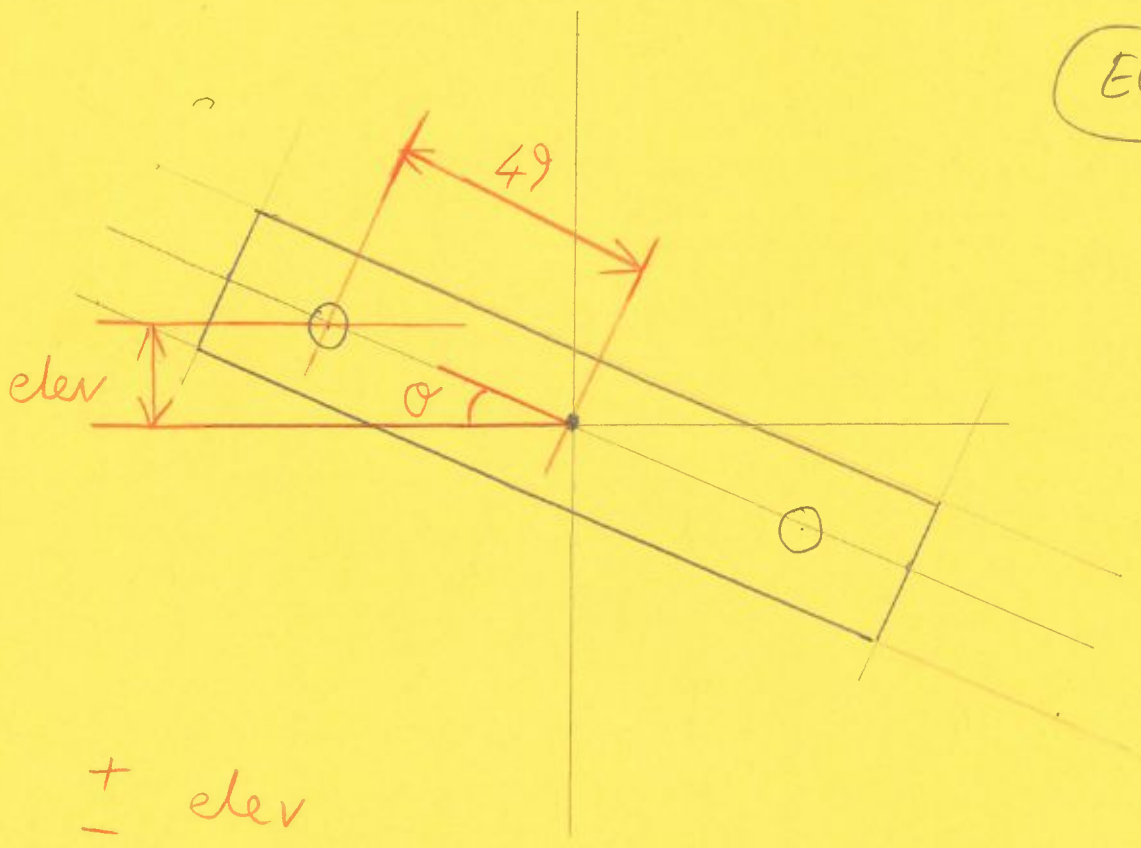
$$= 90 - \left(90 - \frac{\theta'}{2}\right) - \tan^{-1}\left(\frac{\text{forward}}{\text{height}}\right)$$

$$\text{hip}' = \frac{\text{knee}'}{2} - \tan^{-1}\left(\frac{\text{forward}}{\text{height}}\right)$$

Automatically
updated for

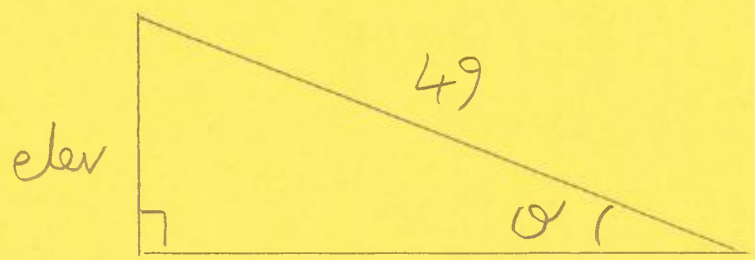
#1

Elev



+ elev
- elev

+ θ
- θ

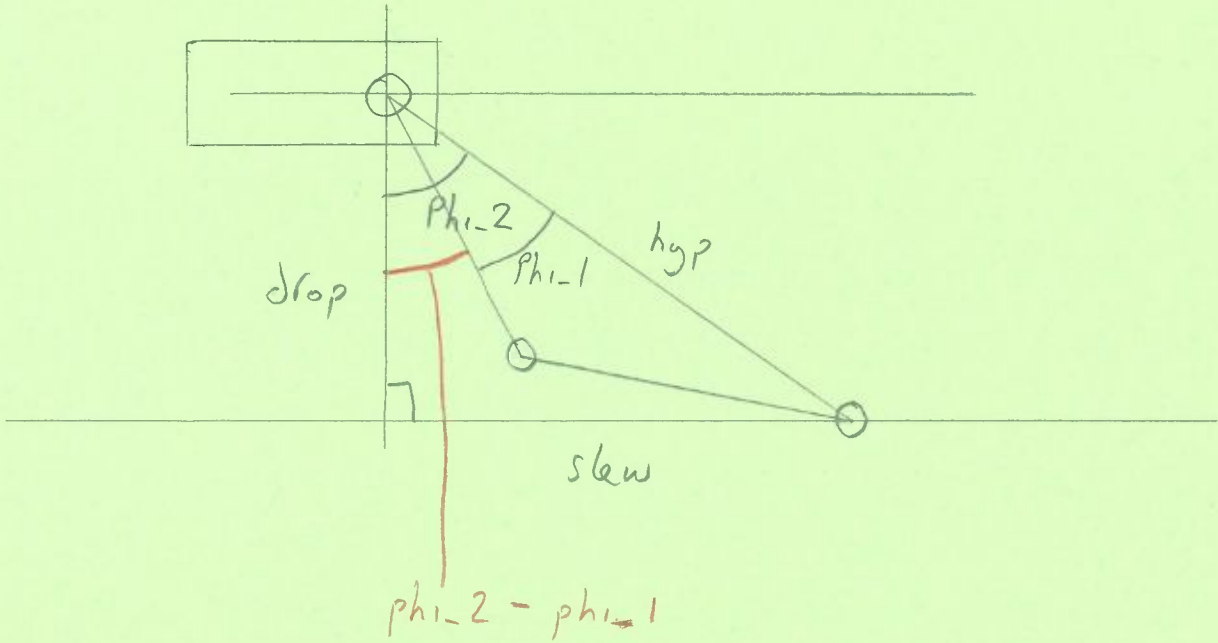


$$\sin \theta = \frac{\text{elev}}{49}$$

$$\theta = \sin^{-1} \left(\frac{\text{elev}}{49} \right)$$

Inverse kinematics

(A)

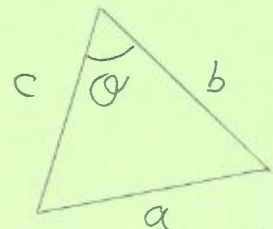


$$\text{drop} = \text{height} - \text{required_height}$$

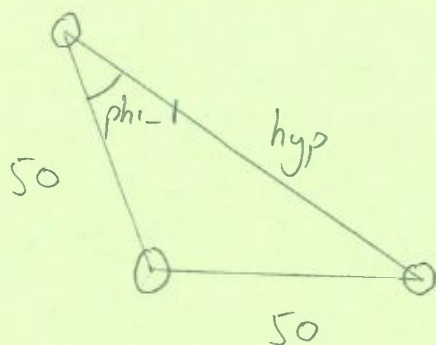
$$\text{hyp} = \sqrt{\text{skew}^2 + \text{drop}^2}$$

Cosine Rule

$$\theta = \cos^{-1} \left[\frac{b^2 + c^2 - a^2}{2bc} \right]$$



(B)



$$\phi_{1-1} = \cos^{-1} \left[\frac{\text{hyp}^2 + 50^2 - 50^2}{2 * \text{hyp} * 50} \right]$$

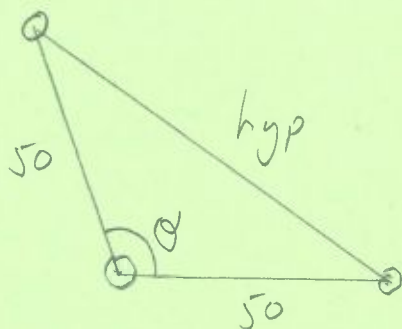
$$\phi_{1-1} = \cos^{-1} \left[\frac{\text{hyp}^2}{100 \text{ hyp}} \right]$$

$$\phi_{1-2} = \tan^{-1} \left[\frac{\text{slen}}{\text{drop}} \right]$$

$$\text{hip} = 90 + (\phi_{1-2} - \phi_{1-1})$$

(C)

Cosine Rule again



$$\text{knee} = \cos^{-1} \left[\frac{50^2 + 50^2 - \text{hyp}^2}{2 * 50 * 50} \right]$$

$$\text{knee} = \cos^{-1} \left[\frac{5000 - \text{hyp}^2}{5000} \right]$$

$$\text{knee} = \cos^{-1} \left[1 - \frac{\text{hyp}^2}{5000} \right]$$

one foot

3 • ↑ 1

Walk

2 • • 4

two feet

↑ •
• ↑

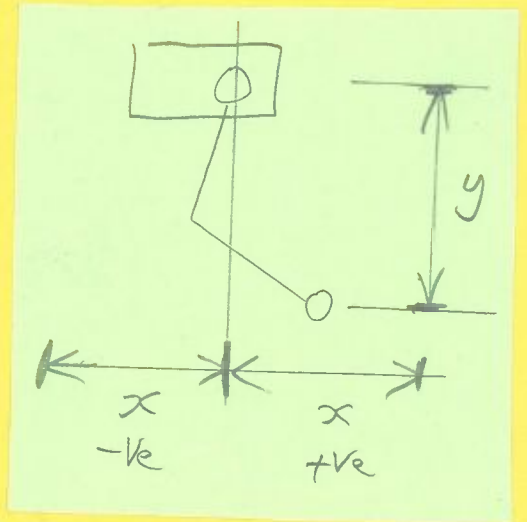
Canter

three feet

trot

four feet

gallop



Kinematics

•
•

set angle of servos →
get to desired foot position

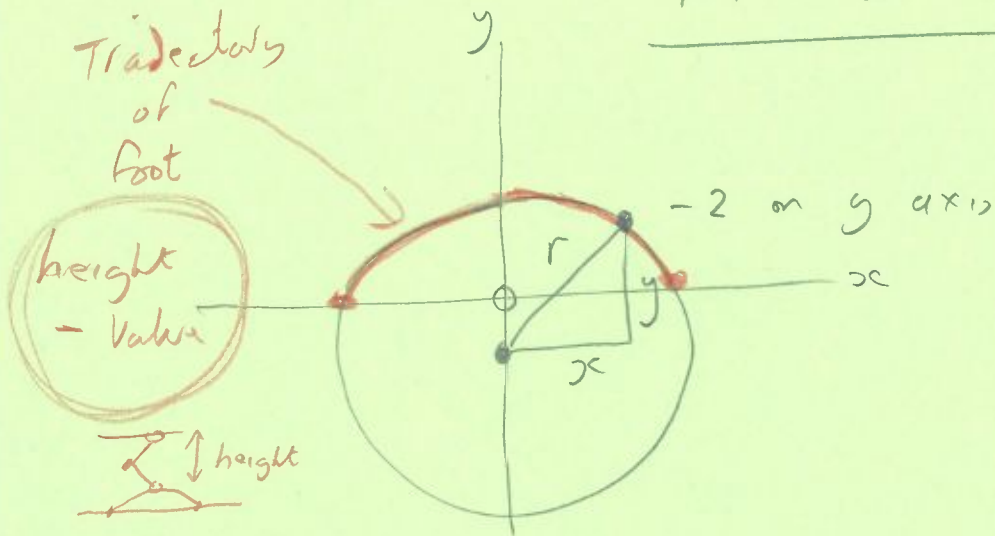
Inverse Kinematics

• set foot end coordinate →
• get angles servos require...

< M7 code >

Python

1m Car Walk



Circle.py

Grid
Centre

$$r^2 = x^2 + y^2$$

$$y^2 = r^2 - x^2$$

$$y = \sqrt{r^2 - x^2}$$

Drop
object
-105
mm

$$y = \left[\sqrt{r^2 - x^2} \right] - 105$$

$r = 60$
mm

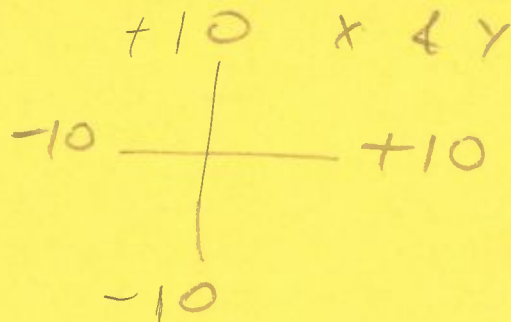
if	$x = \pm 40$:	$y = 60.3 \text{ mm}$
	$x = \pm 20$:	$y = 48.4$
	$x = \pm 10$:	$y = 45.8$
	$x = 0$:	$y = 45.0$

x -40 To +40 mm

@ 1mm Intervals

x = Longitude
y = Latitude

Gyro



Acc = ± 10 Δ x γ

Gyro = Sudden movement
IN REAL TIME
→ Great for Compliance
with soft rubber legs

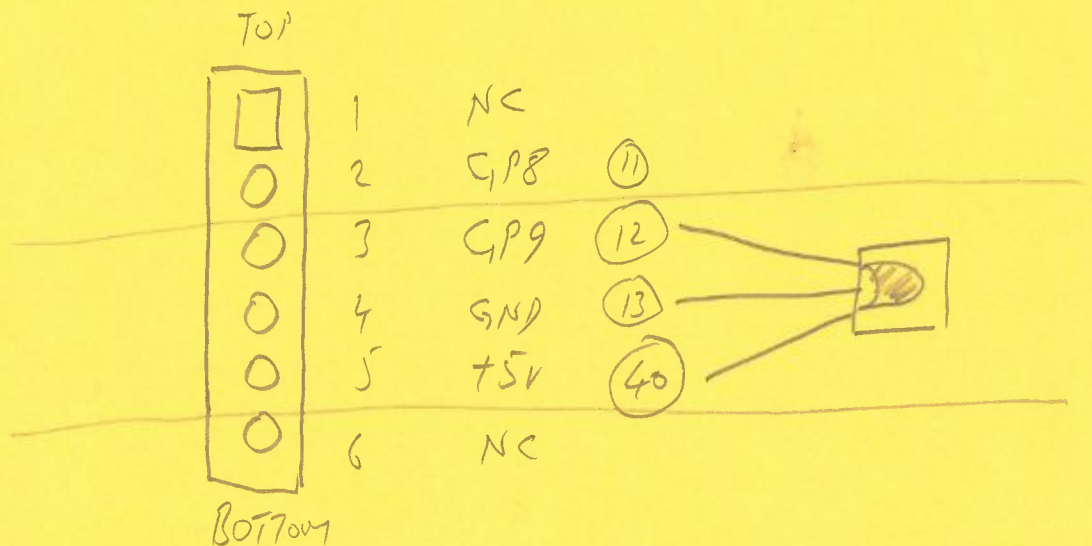
Mag = ? upside down?
COMPASS

So most of time only need **Acc**

IR

V38238

2.5V - 5.5V



The Pi 407 Sensor

Robot Servo Arm MC90S



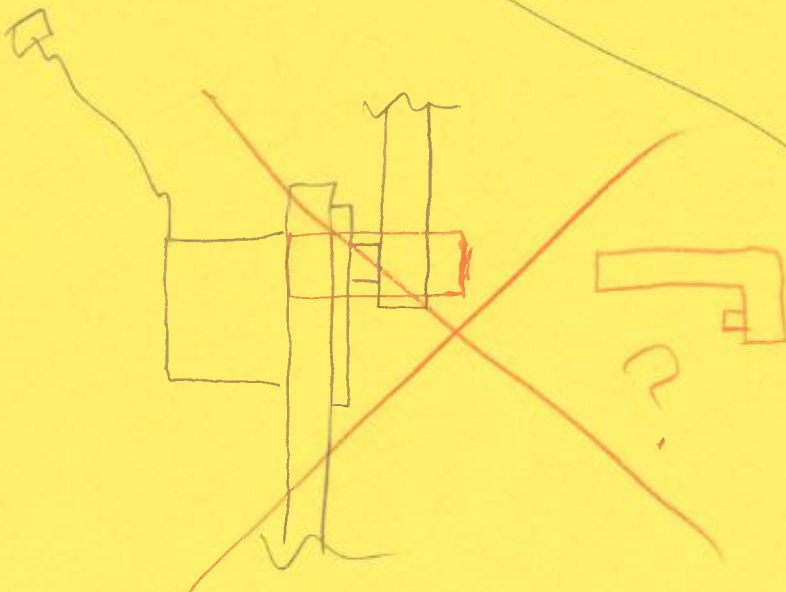
overlapping servo

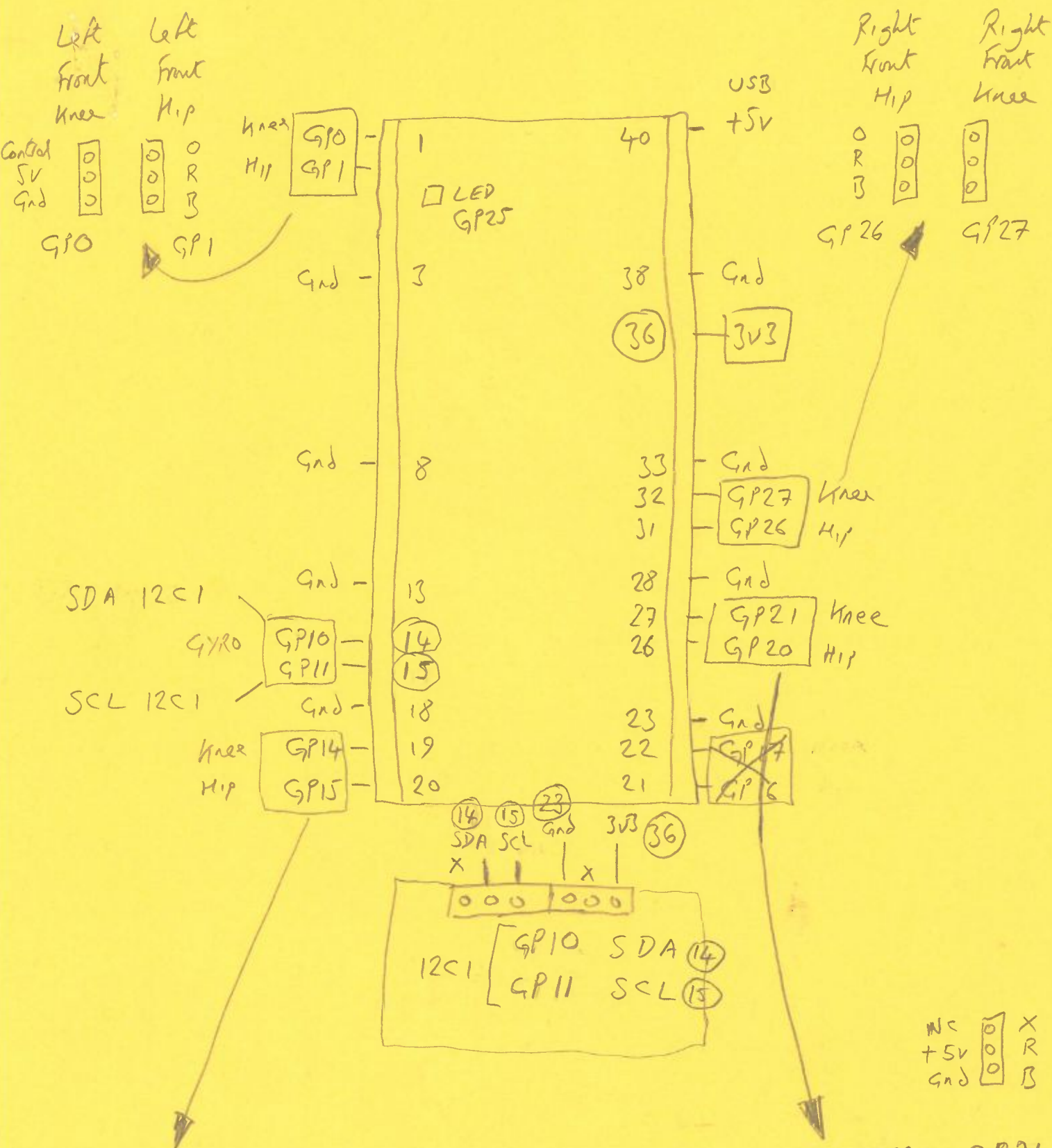


upper leg

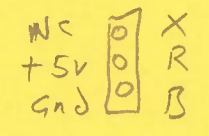
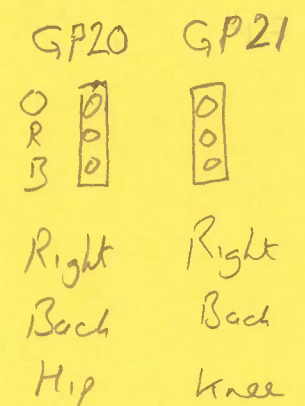
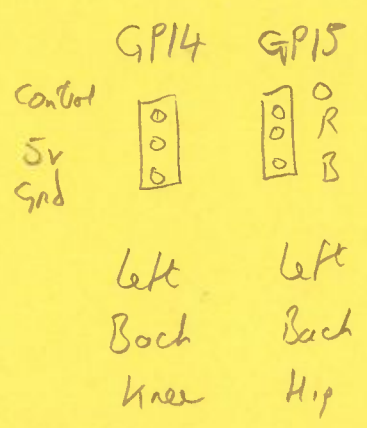


next servo
↳
lower leg?





EACH SERVO PAIR
TO NEAREST
LOCAL GND



FL-knee FL-hip



FRONT

FR-hip FR-knee



GP0 knee

knee GP27

GP1 Hip

Hip GP26

LEFT

GP14 knee

knee GP17 21

GP15 Hip

Hip GP16 20



BL-knee BL-hip

BACK



BR-hip BR-knee

Gyro

12C1

GP10

SDA

GP11

SCL